

Please check that this question paper contains 9 questions and 2 printed pages within first ten minutes.

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Uni. Roll No.

Program/ Course: B.Tech.
Semester: 5th / (2018)
Name of Subject: Theory of Computation
Subject Code: PCIT-112
Paper ID: 16443

15-01-2022(E)

Time Allowed: 02 Hours

Max. Marks: 60

NOTE:

- 1) Each question is of 10 marks.
- 2) Attempt any six questions out of nine
- 3) Any missing data may be assumed appropriately

- Q1. a) State Pumping Lemma for Regular language. Show that the set $L = \{ a^i b^i \mid i \geq 1 \}$ is not regular.
- b) State Pumping Lemma for Context Free Grammar. Show that the set $L = \{ a^p \mid p \text{ is prime} \}$ is not CFL.

- Q2. a) Convert the following Grammar into Greibach Normal Form (GNF):
 $S \rightarrow XA \mid BB, B \rightarrow SB \mid b, X \rightarrow b, A \rightarrow a$

b) Give the examples/applications designed as finite state system.

- Q3. a) Construct a PDA that accepts $L = \{ ww^R \mid w = (a+b)^* \}$. What are the applications of automata theory?

b) State the equivalence of PDA and CFL.

- Q4. a) Differentiate L^* and L^+

b) How many strings of length less than 4 contains the language described by the regular expression $(x+y)^*y(a+ab)^*$?

- Q5. a) How to convert finite automata to regular expression by using Arden's theorem.

b) Suppose that language A_1 has a context-free grammar $G_1 = (V_1, \Sigma, R_1, S_1)$, and language A_2 has a context-free grammar $G_2 = (V_2, \Sigma, R_2, S_2)$, where, for $i = 1, 2, V_i$ is the set of variables, R_i is the set of rules, and S_i is the start variable for CFG G_i . The CFGs have the same set of terminals Σ . Assume that $V_1 \cap V_2 = \emptyset$. Define another CFG $G_3 = (V_3, \Sigma, R_3, S_3)$ with $V_3 = V_1 \cup V_2 \cup \{S_3\}$, where $S_3 \in V_1 \cup V_2$, and $R_3 = R_1 \cup R_2 \cup \{S_3 \rightarrow S_1, S_3 \rightarrow S_2\}$. Argue that G_3 generates the language $A_1 \cup A_2$. Thus, conclude that the class of context-free languages is closed under union.

- Q6. Construct a Turing machine for $L = \{ a^i b^j c^k \mid i*j = k; i, j, k \geq 1 \}$. Discuss the Halting Problem in Theory of Computation.

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Q7. List the Conversion from Mealy to Moore Machine. What is ϵ -closure of a state q_0 ?

Q8. a) Write a regular expression to denote a language L which accepts all the strings which begin or end with either 00 or 11.

b) Construct Pushdown automata for $L = \{0^n 1^m 2^m 3^n \mid m, n \geq 0\}$

Q9. a) Construct a regular expression for the language which accepts all strings with at least two c's over the set $\Sigma = \{c, b\}$

b) What is the minimum number of states in deterministic finite automata (DFA) for string starting with ba^2 and ending with 'a' over alphabet $\{a, b\}$?
